

## SOME FIXED POINT RESULTS IN FUZZY METRIC SPACES USING A CONTROL FUNCTION

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**Abstract.** In this paper, we establish the results on existence and uniqueness of fixed point for  $\phi$ -contractive and generalized C-contractive mapping in the fuzzy metric space in the sense of George and Veeramani. We use the notion of altering distance for proving the results.

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