

PROBABILISTIC NORMS AND STATISTICAL CONVERGENCE OF RANDOM VARIABLES

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Abstract. The paper extends certain stochastic convergence of sequences of \mathbb{R}^k -valued random variables (namely, the convergence in probability, in L^p and almost surely) to the context of E-valued random variables.

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2000 Mathematics Subject Classification: 40A05; 46S50; 54E70.

Keywords: probabilistic norm; random norm; statistical convergence; almost sure convergence.

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