

ABSTRACT. We prove that an arbitrary polycyclic by finite subgroup of $\mathrm{GL}(n, \overline{\mathbb{Q}})$ is up to conjugation virtually contained in a direct product of a triangular *arithmetic* group and a finitely generated diagonal group.