

Erratum

Lower Bounds for Some Factorable Matrices

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The purpose of this erratum is to correct both the mathematical and typographical errors made in 2006.

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The typos are as follows.

- (i) Page 2, line 17, t_0 should read t_0^p .
- (ii) Page 3, line 5, $j = r + 2$ should read $j = r + 1$.
- (iii) Page 3, line 15, Δy_r^p should read Δy_r^p .
- (iv) Page 3, line 16 should read

$$g(r) - g(r + 1) = (r + 2)a_{r+1}^p \Delta y_r^p + (r + 2)\Delta y_r^p \sum_{j=r+2}^{\infty} a_j^p. \quad (1.1)$$

- (v) Page 4, line 7, $q < t < 1$ should read $r > 0$.
- (vi) Page 4, line 11, $v(r)$ should read $u(r)$.
- (vii) Page 6, line 17 $(t^{r+1}/(r + 2))^p$ should read $(t^{r+1}/(r + 2))^p \times$.
- (viii) Page 6, line 18, $=$ should read \times .
- (ix) Page 7, line 6, $-1p]$ should read $-1]$.
- (x) Page 7, line 21 $(n + 1)^{s-1}$ should read $(n + 1)^{1-s}$.
- (xi) Page 8, line 7, $q(p - 1)$ should read $p(p - 1)$.
- (xii) Page 8, line 14, $(r + 1)^{s-1} - (r + 2)^{s-1}$ should read $(r + 1)^{p-1} - (r + 2)^{p-1}$.
- (xiii) Page 8, line 16, $(j + 1)^{(p-1)s}$ should read $(j + 1)^{(s-1)p}$.
- (xiv) Page 10, line 12, $\geq P_r(r + 1)$ should read $\geq 1/(r + 1)$.
- (xv) Page 10, line 14, $(r + 1)P_r^p$ should read $(r + 1)$.

- (xvi) Page 10, line 14, P_{r+1}^p [should read [.
 - (xvii) Page 10, lines 15, 16, P_{r+1}^p [should read P_r^p .
 - (xviii) Page 10, line 17, p_{r+1}/P_r should read $p_{r+1}/P_r)^p$.
 - (xix) Page 12, line 7, $+(r+2)^\alpha$ should read $+(r+2)^{2\alpha}$.
- The mathematical errors occur showing that $\lim_r h(r) = 0$ in Theorems 6 and 7. In Theorem 6, from the formula on line 2 of page 4,

$$\begin{aligned}
 \lim_r h(r) &= \lim_r \frac{a_{r+1}^p \Delta y_r^p}{\Delta^2 y_r^p} \\
 &= \lim_r \frac{[(r+1)^p - (r+2)^p]}{(r+2)^s [(r+1)^p - 2(r+2)^p + (r+3)^p]} \\
 &= \lim_r \frac{(1/(r+2)^s) [1 - ((r+2)/(r+1))^p]}{(1 - 2((r+2)/(r+1))^p + ((r+3)/(r+2))^p)} \\
 &= ((-s/(r+2)^{s+1}) [1 - ((r+2)/(r+1))^p] \\
 &\quad - (-p/(r+2)^s) ((r+2)/(r+1))^{p-1} (-1/(r+1)^2)) \\
 &\quad / (-2p((r+2)/(r+1))^{p-1} (-1/(r+1)^2) \\
 &\quad + p((r+3)/(r+1))^{p-1} (-2/(r+1)^2)) \\
 &= \lim_r ((-s(r+1)^2/2p(r+2)^{s+1}) [1 - ((r+2)/(r+1))^p] \\
 &\quad + (1/(r+2)^s) ((r+2)/(r+1))^{p-1}) \\
 &\quad / (((r+2)/(r+1))^{p-1} - ((r+3)/(r+1))^{p-1}) \\
 &= \lim_r \frac{(-s(r+1)/2p(r+2)^{s+1}) [(r+1)^p - (r+2)^p] + ((r+2)^{p-1}/(r+2)^s)}{(r+2)^{p-1} - (r+3)^{p-1}} \\
 &= \lim_r \frac{(-s(r+1)/2p(r+2)^s) [((r+1)/(r+2))^p - 1] + 1/(r+2)^s}{1 - ((r+3)/(r+2))^{p-1}} \\
 &= \lim_r (-s(r+2)^2/2p) ((r+2 - s(r+1))/(r+2)^{s+1}) ((r+1)/(r+2))^p - 1) \\
 &\quad - (s/2p(r+2)^{s-1}) ((r+1)/(r+2))^p - (s/(r+2)^{s-1}) \\
 &\quad / (p-1) ((r+3)/(r+2))^{p-2} = \lim_r A,
 \end{aligned} \tag{1.2}$$

where

$$A = \frac{-s(r+2 - s(r+1))}{2p(p-1)(r+2)^{s-1}} \left(\left(\frac{r+1}{r+2} \right)^p - 1 \right). \tag{1.3}$$

If $s \geq 2$, then, clearly $\lim_r A = 0$. Suppose that $1 < s < 2$,

$$\begin{aligned} \lim_r A &= \lim_r \frac{(-s/2p(p-1))[(r+1)/(r+2)]^p - 1}{(r+2)^{s-1}/(r+2-s(r+1))} \\ &= \frac{(-s/2)((r+1)/(r+2))^{p-1}}{((r+2)^2(s-1)/(r+2-s(r+1))^2)[r+2-s(r+1)+r+2]} = 0. \end{aligned} \quad (1.4)$$

Thus g is monotone decreasing in r . The balance of the proof of [1, Theorem 6] is correct, and $L^p = f(\infty)$.

In Theorem 7,

$$h(r) = \frac{[(r+1)^p - (r+2)^p]}{(r+1)^p[(r+1)^p - 2(r+2)^p + (r+3)^p]}, \quad (1.5)$$

which is the same h as in Theorem 6, with s replaced by p . Therefore, $\lim_r h(r) = 0$. In the proof of Theorem 7, $g(0) \leq 0$, so $L^p = f(0)$.

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