

A generalisation of fixed point theorems in a 2-metric space ¹

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Abstract

Here we generalise, improve and unify the fixed point theorems due to Delbosco[1], Skof[8], Khan et al.[5] and several other fixed point theorems for a single map and common fixed point theorems ([6], [7]) for a pair of mappings in a setting of 2-metric space.

2000 Mathematics Subject Classification: 47H10, 54H25.

Key words and phrases: metric space, 2-metric space, fixed point, common fixed point

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¹Received 4 April, 2009

Accepted for publication (in revised form) 2 December, 2009

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