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**Zbl 515.05048****Duke, Richard; Erdős, Paul***Subgraphs in which each pair of edges lies in a short common cycle.* (In English)  
**Combinatorics, graph theory and computing, Proc. 13th Southeast. Conf., Boca Raton 1982, Congr. Numerantium 35, 253-260 (1982).**

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$G^k(n, l)$  denotes a  $k$ -graph having  $n$  vertices and  $l$  edges. Theorem 1. For each positive constant  $c$  and sufficiently large  $n$  there exists a positive constant  $c'$  such that each  $G^k(n, cn^k)$  contains  $c'n^{2k}$  distinct copies of the complete  $k$ -partite  $k$ -graph having 2 vertices in each colour class. Corollary 1. For each positive constant  $c$  there exists a positive constant  $c'$  such that for sufficiently large  $n$  each  $G^2(n, cn^2)$  contains a subgraph  $H$  with  $c'n^2$  edges which has the property that each pair of edges of  $H$  are contained in a cycle of  $H$  of length 4 or 6, and each pair of edges which share a common vertex are in a cycle of length 4. An edge  $E$  of a  $k$ -graph  $G^k$  is a separating edge if there exists a partition of the vertices into  $k$  classes such that  $E$  meets each class, but that every other edge of  $G^k$  meets at most  $k - 1$  classes. A  $k$ -cycle is a  $k$ -graph with at least one edge, having no separating edges, and which is minimal with respect to this property. Corollary 2. For each positive constant  $c$  there exists a positive constant  $c'$  such that for sufficiently large  $n$  each  $G^k(c, cn^k)$  contains a sub- $k$ -graph  $H^k$  with the property that each pair of edges of  $H^k$  are contained in a common  $k$ -cycle of  $H^k$ .

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Classification:

05C65 Hypergraphs

05C35 Extremal problems (graph theory)

05C38 Paths and cycles

Keywords:

complete  $k$ -partite sub- $k$ -graph; girth; separating edge