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*Minimal decompositions of two graphs into pairwise isomorphic subgraphs.* (In English)

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[For the entire collection see Zbl 418.00002.]

The basic concept of this paper is that of a U-decomposition. Suppose the edge sets of two graphs  $G$  and  $G'$  can be partitioned into sets  $E_1 + \dots + E_r$  and  $E'_1 + \dots + E'_r$  in such a way that the subgraphs defined by  $E_i$  and  $E'_i$  are isomorphic for  $i=1,2, \dots, r$ . Then this pair of partitions is a U-decomposition of the pair of graphs.  $U(G,G')$  is defined to be the minimum value of  $r$  for which a U-decomposition exists. The paper considers many properties of  $U(G,G')$  and of  $U(n)$  defined as  $\max U(G,G')$  where "max" ranges over all pairs  $(G,G')$  of graphs with  $n$  vertices. The main result of the paper is that  $U(n) = 2n/3 + o(n)$ .

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Classification:

05C35 Extremal problems (graph theory)

Keywords:

isomorphism; edge-chromatic number; edge-dominating number; decomposition